Applied Statistical Analysis EDUC 6050 Week 13

Finding clarity using data



Categorical Outcomes

Categorical Outcomes



General	ID	X	Y
Decuiperente	1	0	0
Requirements	2	2	1
1 0 no no mono	3	1	0
dategorical	4	2	1
variables	5	0	1
	6	0	1
Goodness of Fit	nce	2	0
	8	1	0

Hypothesis Testing with Chi Square (Independence)

The same 6 step approach!

- 1. Examine Variables to Assess Statistical Assumptions
- 2. State the Null and Research Hypotheses (symbolically and verbally)
- 3. Define Critical Regions
- 4. Compute the Test Statistic
- 5. Compute an Effect Size and Describe it
- 6. Interpreting the results

Basic Assumptions

 Independence of data
 Appropriate measurement of variables for the analysis
 Expected frequency 5+

Basic Assumptions

1. Independence of data 2. Appropria Individuals are independent of for be a cach other (one penson's scene)

for the a each other (one person's scores 3. Expected does not affect another's)

Basic Assumptions

 Independence of data
 Appropriate measurement of variables for the analysis
 Expented frequency 5+
 Here we need interval/ratio outcome

Basic Assumptions

Independen
 Approprise
 Approprise
 Whole line

3. Expected frequency 5+

Examining the Basic Assumptions

- **1. Independence:** random sample
- 2. Appropriate measurement: know what your
 variables are
- **3. Expected frequency 5+: Check expected** frequencies

State the Null and Research Hypotheses (symbolically and verbally)

Hypothesis Type	Symbolic	Verbal	Difference between means created by:
Research Hypothesis	$OF \neq EF$	Observed frequency is not equal to expected frequency	True relationship
Null Hypothesis	OF = EF	Observed frequency is the same as the expected frequency	Random chance (sampling error)



How much evidence is enough to believe the null is not true?

generally based on an alpha = .05

Use software's p-value to judge if it is below .05



Compute the Test Statistic

Jamovi

Tutorial



$oldsymbol{\phi}$	Cramer's φ	Estimated Size of the Effect
Close to .1	Depends	Small
Close to .3	on df	Moderate
Close to .5	(pg 557)	Large

Interpreting the results

"The voters' opinions of the president's policies were associated with the voters' political affiliations, $\chi^2(2, N = 58) = 16.40$, p = .02, $\phi = .53$. More democrats and fewer republicans approved of the president's policies than would be expected by chance." – pg 577.

Intro to Logistic Regression

So far, we have always wanted continuous outcome variables

But what if our outcome is a categorical variable??

Logistic Regression is just like linear regression but works with binary (dichotomous) outcomes

- Substance Use or Not
- Cancer or Not
- Buy it or Not

Logic of Logistic Regression



We are trying to find the best fitting S curve

Logic of Logistic Regression



Simple

- Only one predictor in the model
- Tells you if that one predictor is associated with the odds of Y = 1

Multiple

- More than one variable in the model
- Tells you if, while holding the other variables constant, if that predictor is associated with the odds of Y = 1

 Logistic does what regression does but with a little bit of mathematical magic



 Logistic does what regression does but with a little bit of mathematical magic

 $logit(Y) = \beta_0 + \beta_1 X + \epsilon$ intercept

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 Logistic does what regression does but with a little bit of mathematical magic

 $logit(Y) = \beta_0 + \beta_1 X + \epsilon$ intercept unexplained stuff in the odds of Y

slope

$logit(Y) = \beta_0 + \beta_1 X + \epsilon$

Example

We have two variables, X and Y. X is continuous, Y is binary. We want to know if increases/decreases in X are associated (or predict) changes in the chance of Y equaling 1.

- It is trying to predict the outcome accurately using the information from the predictor
- Better prediction tells us that the predictor(s) is/are more strongly related to the outcome

General Requirements

- 1. Two or more variables,
- 2.Outcome needs to be binary
- 3.Others can be continuous or categorical

ID	X	Y
1	8	0
2	6	1
3	9	1
4	7	1
5	7	0
6	8	0
7	5	1
8	5	0

Hypothesis Testing with Logistic Regression

The same 6 step approach!

- 1. Examine Variables to Assess Statistical Assumptions
- 2. State the Null and Research Hypotheses (symbolically and verbally)
- 3. Define Critical Regions
- 4. Compute the Test Statistic
- 5. Compute an Effect Size and Describe it
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Basic Assumptions

 Independence of data
 Appropriate measurement of variables for the analysis
 Normality of distributions
 Homoscedastic

Basic Assumptions

1. Independence of data 2. Appropria Individuals are independent of for the a each other (one person's scores does not affect another's) 4. Homoscedastic

Basic Assumptions

 Independence of data
 Appropriate measurement of variables for the analysis
 Normality of distributions
 Homoran A Here we need nominal outcome

Basic Assumptions

- Independer Residuals should be normally
 Appropria distributed
 - for he analysis
- 3. Normality of distributions
- 4. Homoscedastic

Basic Assumptions

Independence of data Appropriation Variance around the line should for the be roughly equal across the Normalit whole line

4. Homoscedastic

Basic Assumptions

 Independence of data
 Appropriate measurement of variables for the analysis
 Normality of distributions
 Homoscedastic
 Logistic Relationship
 No omitted variables

Basic Assumptions

1. Independence of data

Appropriation of the for the to the data
 Normality of distributions

- 4. Homescedastic
- 5. Logistic Relationships 6. No omitted variables

Basic Assumptions



6.No omitted variables

Examining the Basic Assumptions

- **1. Independence:** random sample
- 2. Appropriate measurement: know what your
 variables are
- 3. Normality: Histograms, Q-Q, skew and kurtosis
- 4. Homoscedastic: Scatterplots
- **5. Logistic:** Scatterplots
- 6.No Omitted: check correlations, know the theory

State the Null and Research Hypotheses (symbolically and verbally)

Hypothesis Type	Symbolic	Verbal	Difference between means created by:
Research Hypothesis	$\beta \neq 0$	X predicts Y	True relationship
Null Hypothesis	$\beta = 0$	There is no <i>real</i> relationship.	Random chance (sampling error)



How much evidence is enough to believe the null is not true?

generally based on an alpha = .05

Use software's p-value to judge if it is below .05



Compute the Test Statistic

						OfficeParks	
	☰ Data	Analyses					
	-		2 00	0			
	_	<u>የ</u> ት 🔁					
	Exploration T-Te	sts ANOVA Regi	ession Frequencies	Factor			
	. nom	A prod1 Co	rrelation Matrix	o 🔶 ma	arr 🔶 good		
				o v 1110			
	2 Pom	2 Lir	lear Regression	7	1		
	2 Fam	Logis	tic Regression	7	1		
	4 Dwight	5 2	Outcomes	8	0		
	5 Stanley		Binomial	4	1		
	6 Phyllis	4 N	Outcomes	4	1		
	treed	1	Multinomial	4	0		
Click on	leredith	3	5	4	0		
	lscar	5	7	7	0		
"2 Outcomes	ngela	4	5	7	0		
	levin	2	6	2	0		
Binomial	ellev	3	5	5	0		
	IS I Ivan	2	2	5	0		
	14 Toby	4	1	6	0		
	15 Andy	3	5	7	0		
	16 Jan	4	6	6	1		
	17 April	1	6	4	1		
	18 Andy	1	2	2	1		
	19 Leslie	5	8	7	0		
	20 Ron	3	8	7	0		
	21 Tom	2	5	5	0		
	22 Donna	2	7	6	0		
	23 Ben	5	8	5	0		
	24 Chris	4	6	8	0		
	25 Gary (Larry,	3	5	3	1		
	26 Jean Ralphio	1	1	2	0		
	27 Mona Lisa	1	1	1	0		
	28 Ann	5	8	8	0		
	29 Kyle	3	5	2	1		
						()	



larginal Means

> Prediction



OfficeParks



Model Coefficients

95% Confidence

Interval

Predictor	Estimate	SE	Z	р	Odds ratio	Lower	Upper
Intercept	2.1381	1.3809	1.55	0.122	8.483	0.566	127.060
Income	-0.0805	0.0333	-2.42	0.016	0.923	0.864	0.985

Note. Estimates represent the log odds of "subs = 1" vs. "subs = 0"

Estimate in "log-odds" units

Significant

The odds ratio is below 1 so as income increases, the odds of using substances decreases by ~1 - .923 = .077 (7.7% decrease)



Continuous Predictor





Categorical Predictor

Model Coefficients

						95% Confidence Interval		
Predictor	Estimate	SE	Z	р	Odds ratio	Lower	Upper	
Intercept	-1.504	0.553	-2.721	0.007	0.222	0.0752	0.657	
Show:								
The Office – Parks and Rec	0.405	0.799	0.507	0.612	1.500	0.3131	7.186	
Noto Estimatos	ropresent the	log odds o [.]	f "subs = 1" י	vs. "subs = (ר"			
Estimate in "	log-odds" u	nits		The odds The Offic	ratio is ab e have an o	ove 1 so dds of us	individuals ing substa	
	Ν	lot Signif	icant	50% (1.	5 - 1 = .5	= 50%) hi	gher than I	



Categorical Predictor



5 Compute an Effect Size and Describe it

One of the main effect sizes for regression is R^2 $Odds Ratio = \frac{Odds \ of \ Y \ when \ X \ is \ one \ unit \ higher}{Odds \ of \ Y \ when \ X \ is \ not \ one \ unit \ higher}$

6 Interpreting the results

The logistic regression analysis showed that income significantly predicted the odds of substance use (OR = .923, p = .016). As income increased by \$1000, the odds of using substances decreased by 7.7%.

Multiple Logistic Regression

Multiple Logistic Regression

More than one predictor in the same model

This change the interpretation just a little:

Slope is now the change in the odds of
Y = 1 for a one unit change in X, while
holding the other predictors constant.

Multiple Regression

Provides us with a few more things to think about

- **1. Variable Selection**
- 2. Assumption Checks (much more difficult in logistic regression)
- 3. Multi-collinearity
- 4. Interactions

Variable Selection

Several Approaches

- 1. Forward
- 2. Backward
- 3. Lasso
- 4. Covariates then predictor of interest

Variable Selection when theory isn't clear

Several Approaches

- 1. Forward
- 2. Backward
- 3. Lasso

4. Covariates then predictor of interest

I'd recommend these two

Assumption Checks

Difficult (we won't cover it in this class)

Jamovi doesn't provide many checks
(only collinearity)

Multi-Collinearity

When two or more predictors are very related to each other or are linear combinations of each other

Check correlations Dummy codes are correct (Jamovi does this automatically)

Interactions

Just as we do in linear models

Can have 2+ variables in the interaction



Interactions

	•				0	fficeParks						
	☰ Data	Analyses										
	Exploration T-Test	s ANOVA Regression	on Frequenci	ies Factor								Module
	Binomial Log	gistic Regression			$\overline{\rightarrow}$	Estimat sho	ed Marginal M w	eans				
	 All Co Chil alco spor depr1 awkw1 		Fact	tors show Married			1.00 - 0.75 -					
	prod2 Model Build Predictors show	er	Bloc	ock 1			U.25 -	T		Ţ		
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			All 2 way All 3 way All 4 way	d New Block			Estimated Margir	nal Means - sho	shov	V 95% Confide	nce Interval	
Can tell Jamovi an interaction	to do	evels Checks	All 5 way				show Parks and Rec The Office	Probability 0.138 0.191	SE 0.0834 0.1085	Lower 0.0387 0.0564	Upper 0.387 0.483	
	🗸 Model Fit											

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Questions? Please post them to the discussion board before class starts

End of Pre-Recorded Lecture Slides

In-class discussion slides



Application

Example Using The Office/Parks and Rec Data Set

> Hypothesis Test with Logistic Regression